

## JOHN CABOT UNIVERSITY

COURSE CODE: MA 495 COURSE NAME: Differential Equations Summer Sample Syllabus

TOTAL NO. OF CONTACT HOURS: 45 CREDITS: 3 PREREQUISITES: MA 299, MA 491 (Multivariable calculus and Matrix Algebra)

### **COURSE AIMS:**

This course provides an introduction to ordinary differential equations. These equations contain a function of one independent variable and its derivatives. The term "*ordinary*" is used in contrast with the term partial differential equation which may be with respect to *more than* one independent variable.

#### **COURSE SUMMARY:**

Ordinary differential equations and applications, with integrated use of computing, student projects; first-order equations; higher order linear equations; systems of linear equations, Laplace transforms; introduction to nonlinear equations and systems, phase plane, stability.

### **LEARNING OUTCOMES:**

Upon successful completion of this course, the student will:

- 1. solve first order linear equations including the method of integrating factors
- 2. solve non-linear equations, in particular separable and exact equations
- 3. solve second-order linear constant coefficient equations, both homogeneous and non-homogeneous including methods of characteristic equations, undetermined coefficients, and variation of parameters
- 4. learn generalization of the techniques for second order to higher order linear constant coefficient equation, both homogeneous and nonhomogeneous
- 5. learn Laplace Transform methods, including solutions of second order problems with discontinuous forcing and impulse response
- 6. solve systems of first-order linear constant coefficient equations, both homogeneous and non-homogeneous. This includes solutions of



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homogeneous problems using eigenvalues as well as extensions of the methods of undetermined coefficients and variation of parameters for non-homogeneous problems.

**TEXTBOOK:** Boyce, Di Prima, and Haines. Elementary Differential Equations and Elementary Differential Equations w/Boundary Value Problems, 10 Edition, John Wiley & Sons.

### **GRADING POLICY**

#### -ASSESSMENT METHODS:

Assignment	Guidelines	Weight
Homework	Homework assignments will be graded: the average grade weighs 10 percent of the final grade.	10%
Quizzes	Every week, starting from the second week, students will be asked to solve and hand in a simple, fifteen-to-twenty- minute quiz. The average quiz score weighs fifteen percent of the final grade.	25%
Mid-term exam		25%
Final exam (comprehensive)		40%

### LIST OF TOPICS COVERED

Classification of differential equations; direction fields; exponential growth and decay; related physical phenomena; linear equations and integrating factors; separate equations; reduction of order, application of nonlinear equations: Bernoulli and logistic equations, gravitation; sample computer lab assignment; direction fields; integration and differentiation; solution of first-order differential equations and initial value problems. Mechanical and electrical oscillation: modeling by initial value problems; linear, constant-coefficient second-order equations; homogeneous case; the characteristic polynomial; method of undetermined coefficients; oscillation and resonance (plus amplitude modulation and other phenomena); the Laplace transform L; definition and foundations; table entries; first differential rule; solving initial value problems using Laplace and inverse Laplace; sample computer assignment: Laplace transform (beyond constant-coefficient equations and beyond the familiar table entries); undetermined coefficients; amplitude modulation; more on the Laplace transform: first and second shift rules; second differentiation; more place transform impulse



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response; transfer function; linearity; the Wronskian; use of a known homogeneous solution to find another; variation of parameters; systems: generalities, reduction of higher-order equations to first-order systems; linear systems: homogenous with constant coefficients; eigenvalues; the cases of complex and repeated eigenvalues; non-homogeneous systems; equilibria and stability, phase plane dynamics for two dimensional systems.